

Notes 3.3B

Graphing Linear Equations Using  
Intercepts

# Steps to Graphing Using Intercepts

- 1. Find both the  $x$ - and  $y$ -intercepts.
- 2. Plot the intercepts on the graph.
- 3. Connect the intercepts with a line.

To Check:

Find a third set of coordinate points using a table. The third point should be on the line.

# I. Finding the $x$ - and $y$ -intercepts.

## A. Finding the $x$ -intercept

- For the equation  $2x + y = 6$ , we know that  $y$  must equal 0. What must  $x$  equal?
- Substitute in 0 for  $y$  and simplify.  
$$2x + 0 = 6$$
$$2x = 6$$
$$x = 3$$
- So  $(3, 0)$  is the  $x$ -intercept of the line.

## B. Finding the $y$ -intercept

- For the equation  $2x + y = 6$ , we know that  $x$  must equal 0. What must  $y$  equal?

- Substitute in 0 for  $x$  and simplify.

$$2(0) + y = 6$$

$$0 + y = 6$$

$$y = 6$$

- So  $(0, 6)$  is the  $y$ -intercept of the line.

## To summarize....

- To find the  $x$ -intercept, substitute in 0 for  $y$ .
- To find the  $y$ -intercept, substitute in 0 for  $x$ .

## II. Graphing Using Intercepts

1. Find the  $x$  and  $y$ - intercepts  
of  $x = 4y - 5$ . Graph the equation.

Step 1: Find the intercepts.

- **$x$ -intercept:**

- Plug in  $y = 0$

$$x = 4y - 5$$

$$x = 4(0) - 5$$

$$x = 0 - 5$$

$$x = -5$$

- $(-5, 0)$  is the  
 $x$ -intercept

- **$y$ -intercept:**

- Plug in  $x = 0$

$$x = 4y - 5$$

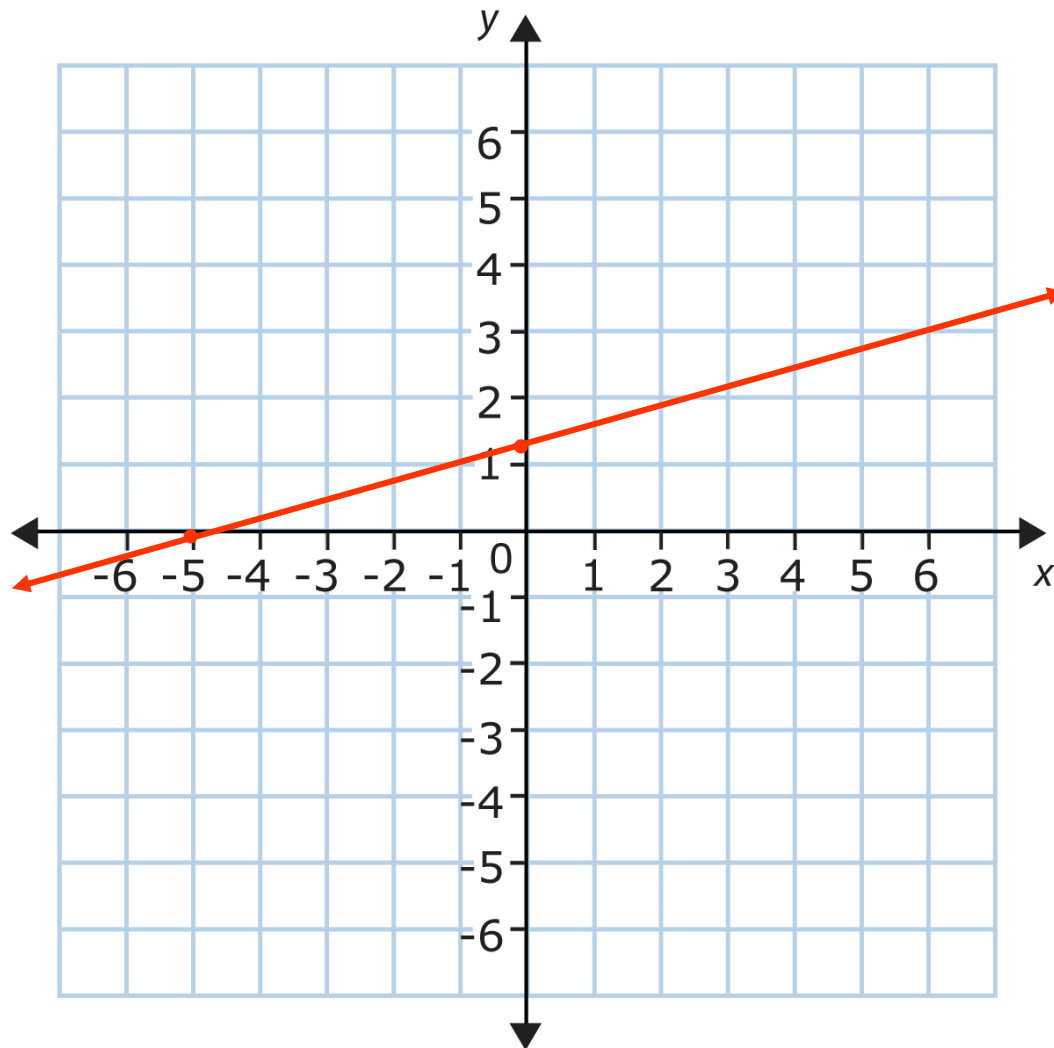
$$0 = 4y - 5$$

$$5 = 4y$$

$$\frac{5}{4} = y$$

- $(0, \frac{5}{4})$  is the  
 $y$ -intercept

Step 2: Plot the intercepts



Step 3: Connect the intercepts with a line

## 2. Find the $x$ and $y$ -intercepts of $g(x) = -3x - 1$ \*

- **$x$ -intercept**

- Plug in  $y = 0$

$$g(x) = -3x - 1$$

$$0 = -3x - 1$$

$$1 = -3x$$

$$-\frac{1}{3} = x$$

- $(-\frac{1}{3}, 0)$  is the  
 $x$ -intercept

\* $g(x)$  is the same as  $y$

- **$y$ -intercept**

- Plug in  $x = 0$

$$g(x) = -3(0) - 1$$

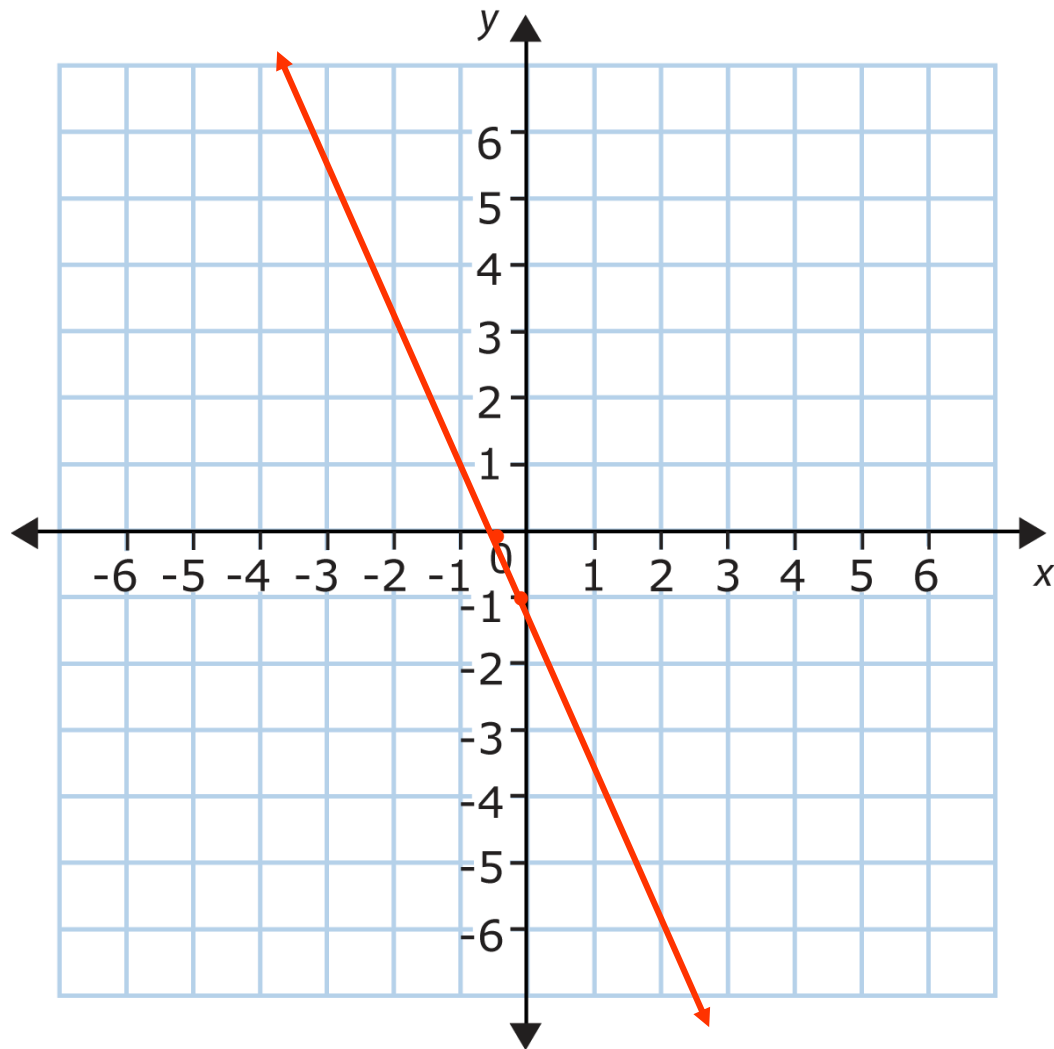
$$g(x) = 0 - 1$$

$$g(x) = -1$$

- $(0, -1)$  is the  
 $y$ -intercept



Step 2: Plot the intercepts



Step 3: Connect the intercepts with a line

### 3. Find the $x$ and $y$ -intercepts of

$$6x - 3y = -18$$

- **$x$ -intercept**

- Plug in  $y = 0$

$$6x - 3y = -18$$

$$6x - 3(0) = -18$$

$$6x - 0 = -18$$

$$6x = -18$$

$$x = -3$$

- $(-3, 0)$  is the  $x$ -intercept

- **$y$ -intercept**

- Plug in  $x = 0$

$$6x - 3y = -18$$

$$6(0) - 3y = -18$$

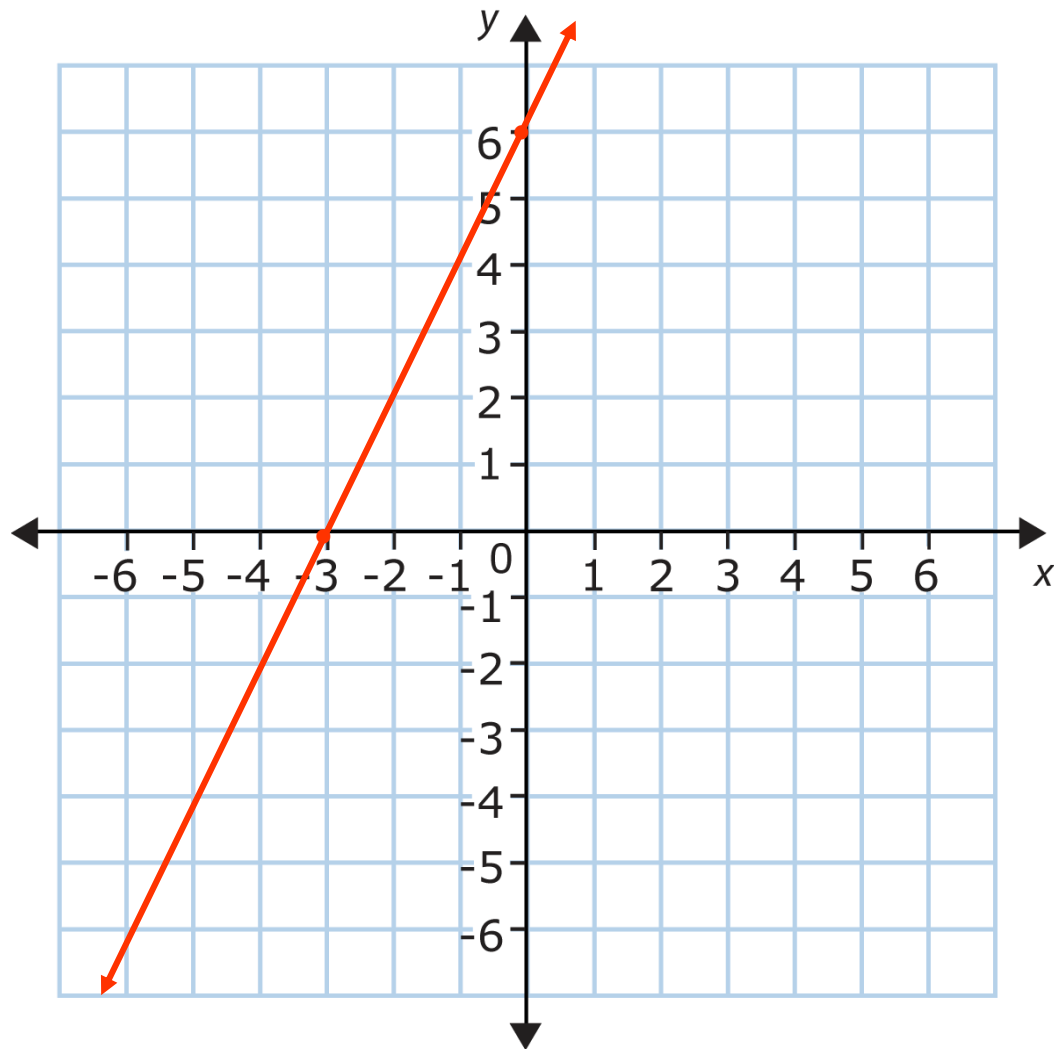
$$0 - 3y = -18$$

$$-3y = -18$$

$$y = 6$$

- $(0, 6)$  is the  $y$ -intercept

Step 2: Plot the intercepts



Step 3: Connect the intercepts with a line

## 4. Find the $x$ and $y$ -intercepts of $x = 3$

- **$x$ -intercept**

- Plug in  $y = 0$ .

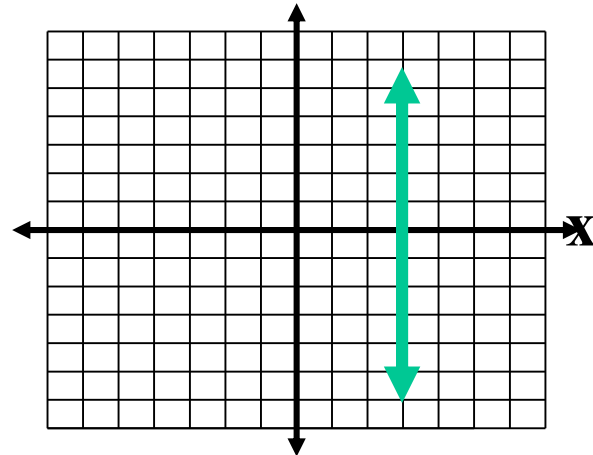
There is no  $y$ . Why?

- $x = 3$  is a **vertical** line so  $x$  always equals 3.
- $(3, 0)$  is the  $x$ -intercept.

- **$y$ -intercept**

- A vertical line never crosses the  $y$ -axis.

- There is no  $y$ -intercept.



## 5. Find the $x$ and $y$ -intercepts of $y = -2$

- **$x$ -intercept**
- Plug in  $y = 0$ .  
 $y$  cannot = 0 because  
 $y = -2$ .
- $y = -2$  is a **horizontal**  
line so it never crosses  
the  $x$ -axis.
- There is no  $x$ -intercept.

- **$y$ -intercept**
- $y = -2$  is a horizontal line  
so  $y$  always equals  $-2$ .
- $(0, -2)$  is the  $y$ -intercept.

